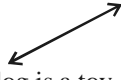


19. (1) First Premise is Particular Affirmative (I-type).
Second Premise is Universal Negative (E-type).

Some cats are dogs.



No dog is a toy.

I + E ⇒ O – type of Conclusion.

“Some cats are not toys.”

This is Conclusion III.

Conclusion I is Converse of the first Premise.

20. (2) L.C.M. of 6, 5, 7, 10 and 12 is 420.
So, the bells will ring together after every 420 seconds
i.e. 7 minutes.
Now, $7 \times 8 = 56$ and $7 \times 9 = 63$.
Thus, in 1 hour (or 60 minutes), the bells will toll
together 8 times, excluding the one at the start.

- 54 (3)
55 (4)
56 (3)
57. (3)

$$= \left(\frac{2}{\sin \theta} - 3 \sin \theta \right)^2 + 2 \cdot \frac{2}{\sin \theta} \cdot 3 \sin \theta$$

$$= \left(\frac{2 - 3 \sin^2 \theta}{\sin \theta} \right)^2 + 12$$

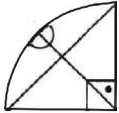
For the least value $\left(\frac{2 - 3 \sin^2 \theta}{\sin \theta} \right)$ would be 0 (zero).

∴ The least value = 12

We may consider that (1800 – 1650) gives interest of 30 at 4% per annum.

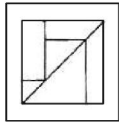
$$\therefore \text{Time} = \frac{30 \times 100}{150 \times 4} = 5 \text{ years}$$

21. (2)



- 22 (3)
23 (2)
24 (3)

25. (4)



- 51 (1)

52. (2) Let speed of boat = x, speed of current = y
Downstream speed = (x + y),
upstream speed = (x – y)
Condition (i):

$$\frac{21}{x+y} + \frac{21}{x-y} = 10 \quad \dots(1)$$

Condition (ii):

$$\frac{7}{x+y} = \frac{3}{x-y} \Rightarrow \frac{x+y}{x-y} = \frac{7}{3}, \text{ assume } x+y=7k,$$

(x – y) = 3k, put values in equ. (1)

then, k = 1, x + y = 7, x – y = 3

$$\text{speed of boat} = \frac{7+3}{2} = 5 \text{ km/h}$$

$$\text{speed of current} = \frac{7-3}{2} = 2 \text{ km/h}$$

53. (1) $4 \operatorname{cosec}^2 \theta + 9 \sin^2 \theta = \frac{4}{\sin^2 \theta} + 9 \sin^2 \theta$

$$= \left(\frac{2}{\sin \theta} \right)^2 + (3 \sin \theta)^2 \quad \because a^2 + b^2 = (a-b)^2 + 2ab$$

58. (4) x = y

$$\Rightarrow 2t = \frac{2t-1}{3} \Rightarrow 6t = 2t-1 \Rightarrow 4t = -1$$

$$\Rightarrow t = -\frac{1}{4}$$

- 59 (1)

60. (2) Given $x = \frac{\sqrt{3}}{2}$

$$\frac{\sqrt{1+x}}{1+\sqrt{1+x}} \times \frac{1-\sqrt{1+x}}{1-\sqrt{1+x}} + \frac{\sqrt{1-x}}{1-\sqrt{1-x}} \times \frac{1+\sqrt{1-x}}{1+\sqrt{1-x}}$$

$$= \frac{\sqrt{1+x}-1-x}{1-1-x} + \frac{\sqrt{1-x}+1-x}{1-1+x}$$

$$= \frac{\sqrt{1-x}+1-x}{x} - \frac{\sqrt{1+x}-1-x}{x}$$

$$= \frac{\sqrt{1-x}+1-x-\sqrt{1+x}+1+x}{x}$$

$$= \frac{2+\sqrt{1-x}-\sqrt{1+x}}{x} = \frac{2+\sqrt{1-\frac{\sqrt{3}}{2}}-\sqrt{1+\frac{\sqrt{3}}{2}}}{\frac{\sqrt{3}}{2}}$$

$$= \frac{2+\frac{\sqrt{4-2\sqrt{3}}}{2}-\frac{\sqrt{4+2\sqrt{3}}}{2}}{2}$$

$$= \frac{\sqrt{3}}{2}$$

$$= \frac{4+\sqrt{3}-1-\sqrt{3}-1}{\sqrt{3}} = \frac{2}{\sqrt{3}}$$

61. (2) Let x is the no. of individuals who were covered. Then,

Percentage of uncertain individuals

$$= [100 - (20 + 60)]\% = 20\%$$

$$\therefore 60\% \text{ of } x - 20\% \text{ of } x = 720$$

$$\Rightarrow 40\% \text{ of } x = 720$$

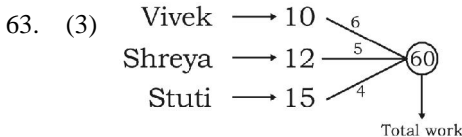
$$\Rightarrow \frac{40}{100}x = 720 \Rightarrow x = \left(\frac{720 \times 100}{40}\right) = 1800.$$

62. (1) Runs in the first match = 150

$$\text{Runs in the second match} = \frac{150}{5} \times 6 = 180$$

$$\text{Runs in the third match} = \frac{180}{4} \times 3 = 135$$

$$\text{Required average} = \frac{150 + 180 + 135}{3} = 155$$



Vivek leaves after 2 days so remaining work

$$= 60 - 12 = 48$$

and last three days stuti work alone

$$\therefore \text{Remaining work ? } 60 - 12 + 15 = 63$$

$$\therefore \text{Required time} = \frac{63}{9} = 7 \text{ days}$$

$$\text{Total days} \rightarrow 4 + 3 = 7$$

64. (2)

65. (3) Side of the first square

$$= \sqrt{\text{Area}} = \sqrt{200} = 10\sqrt{2} \text{ metre}$$

$$\text{Its diagonal} = \sqrt{2} \times \text{side} = 10\sqrt{2} \times \sqrt{2} = 20 \text{ metre}$$

\therefore Diagonal of new square

$$= \sqrt{2} \times 20 = 20\sqrt{2} \text{ metre}$$

$$\therefore \text{Its area} = \frac{1}{2} \times (\text{diagonal})^2$$

$$= \frac{1}{2} \times 20\sqrt{2} \times 20\sqrt{2} \text{ m} = 400 \text{ sq. metre}$$

66. (4) Area of the base = $\frac{\sqrt{3}}{4} \times (\text{side})^2$

$$= \frac{\sqrt{3}}{4} \times 6 \times 6 = 9\sqrt{3} \text{ sq. cm.}$$

\therefore volume of the prism = Area of the base \times height

$$\Rightarrow 108\sqrt{3} = 9\sqrt{3} \times h$$

$$\Rightarrow h = \frac{108\sqrt{3}}{9\sqrt{3}} = 12 \text{ cm}$$

67. (3)

68. (1) Let the amount (sum) deposited for the two sons are A and B respectively.

ATQ,

$$A \left(1 + \frac{4}{100}\right)^5 = B \left(1 + \frac{4}{100}\right)^7$$

$$\Rightarrow \frac{A}{B} = \left(1 + \frac{4}{100}\right)^2 = \left(\frac{26}{25}\right)^2 = \frac{676}{625}$$

$$\therefore (676 + 625) \text{ units} = 2602$$

$$1301 \text{ units} = 2602$$

$$1 \text{ unit} = 2$$

Amount deposited into the account of 1st son

$$= 676 \times 2 = 1352$$

69. (3) $ax^2 + bx + c = a(x - p)^2$

$$ax^2 + bx + c = a(x^2 - 2px + p^2)$$

$$ax^2 + bx + c = ax^2 - 2apx + ap^2$$

On comparison, we get

$$b^2 = 4a^2 p^2 \text{ and } p^2 = \frac{c}{a}$$

$$\Rightarrow p^2 = \frac{b^2}{4a^2} \Rightarrow \frac{b^2}{4a^2} = \frac{c}{a}$$

$$\Rightarrow \boxed{b^2 = 4ac}$$

70. (3)

71. (3) Required number of students passed in third division = 70

72. (3) Percentage of students failed in 1984

$$= \frac{35}{200} \times 100 = 17\frac{1}{2}\%$$

73. (3) Total passed students = 140 + 150 + 165 = 455

$$\text{Total students} = 170 + 195 + 200 = 565$$

\therefore Required percentage

$$= \frac{455}{565} \times 100 = \frac{9100}{113} = 80\frac{60}{113}\%$$

74. (4) Required percentage = $\frac{20}{170} \times 100 = \frac{200}{17} = 11\frac{13}{17}\%$

75. (4) Required percentage = $\frac{140}{170} \times 100 = \frac{1400}{17} = 82\frac{6}{17}\%$